

# Assignment 2

## COMP6741: Parameterized and Exact Computation

2017, Semester 2

Assignment 2 is based on group work. Each group consists of 3 students (group sizes of 2–4 are acceptable). Post on the Forum if you are looking for a group to join, or if your group is short of members.

If any works (articles, Wikipedia entries, lecture notes, etc.) inspired your solutions, please cite them and give a list of references at the end of your report.

If you have questions about this assignment, please post them to the Forum.

**Due date.** This assignment is due on Wednesday, 20 September 2017, at 23.59 AEST. Submitting  $x$  days after the deadline, with  $x > 0$ , reduces the grade by  $20 \cdot x$  per cent.

**Submission.** One group member submits a TAR(.GZ) or ZIP archive with the following files:

- a report in PDF format (the first page should contain the names and Student IDs of each group member), and
- all source files of the implementations,
- a statically-linked executable of the implementation, and
- two shell scripts `mycompile.sh` and `myrun.sh` such that `mycompile.sh` compiles the code (in case you use an interpreted language, this shell script might simply do nothing), and `myrun.sh` executes the algorithm implementation with default parameters on an instance that you provide.

Submit this archive using the command

```
give cs6741 a2 <myarchive>
```

from the CSE network, or use the WebCMS3 frontend for `give`.

Size limit: 50 Megabytes

## Assignment

This assignment centers around the Boolean Satisfiability problem and focuses on practical aspects.

SATISFIABILITY (SAT)

Input: A Boolean formula  $F$  in conjunctive normal form.

Question: Is there an assignment  $\alpha : \text{var}(F) \rightarrow \{0, 1\}$  to the variables of  $F$  for which  $F$  evaluates to 1?

## Literature review

The first part of the assignment is a literature review. Your descriptions and explanations of procedures/algorithms should be detailed enough so that a typical COMP6741 student can implement them based only on your description. If there are multiple variants of a given concept, it is sufficient to describe only one variant.

1. Describe the unit clause simplification rule, also known as unit propagation (UP). Give an example of a SAT instance where UP can be applied. [5 points]
2. Describe the pure literal rule (PL). Give an example of a SAT instance where PL can be applied. [5 points]
3. Describe the concept of random restarts. [5 points]
4. Describe two variable selection heuristics, for choosing a variable to branch on (and maybe to decide which value we assign to the variable in the first branch). [10 points]
5. Describe Conflict-Driven Clause Learning (CDCL), including any other needed concepts, such as implication graphs. Give an example of a SAT instance and an execution of a CDCL algorithm where CDCL helps to decrease the size of the search tree. [25 points]

## Implementation, experiments, and interpretation of results

Implement a CDCL algorithm for SAT using a common programming language such as C, C++, Python, or Java. It is recommended to base your implementation on an existing solver, such as the open-source solver MiniSAT.

Choose a set of benchmark instances. A good source of benchmark instances are the SAT competitions.

Describe your test environment, time-outs (if no solution is found after, e.g., 5 minutes, stop the algorithm), memory limit (should be around 1-4 Gigabytes), and how you simulate the generation of random choices.

- Quality of code and selection of benchmark instances. [20 points]
- Reproducibility of results: it should be easy for anyone with access to your report, your code, and an internet connection to reproduce your results. [10 points]
- Run variants of your implementation on your benchmark instances to try to answer the following questions:
  1. How much does conflict-driven clause learning help in SAT solving? Compare no CDCL, a small amount of CDCL, and a large amount of CDCL.
  2. How much do the simplification rules UP and PL help? Compare only UP, only PL, simplification rules only at every  $k$ th level of the search tree (for  $k = 2$  or  $k = 3$ ), or an exhaustive use of simplification rules.
  3. Which variable selection heuristic performs better?

What conclusions do your experiments allow you to make for these questions? [20 points]

**Bonus question.** What structure or properties do instances have where the unsuccessful strategies above actually performed better? [5 points]