

# Exercise Sheet 1

## COMP6741: Parameterized and Exact Computation

2016, Semester 2

1. Arrange the following functions in increasing order of growth:  $n^{\log n}$ ;  $(\log n)^n$ ;  $2^n$ ;  $2^{2^n}$ ;  $2^{n^2}$ ;  $n!$ ;  $1.01^n$ ;  $50^n$ ;  $2^{n/2}$ ;  $2^{\sqrt{n}}$ .
2. Show that VERTEX COVER can be solved in polynomial time for graphs of maximum degree at most 2.
3. A vertex cover  $C$  of a graph  $G$  is *minimal* if no strict subset of  $C$  is a vertex cover. Show that any graph has at most  $2^k$  minimal vertex covers of size at most  $k$ . Furthermore, show that given  $G$  and  $k$ , all minimal vertex covers of  $G$  of size at most  $k$  can be enumerated in time  $2^k n^{O(1)}$ .