Lab 3

COMP9021, Session 2, 2015

1 Finding particular sequences of prime numbers

Write a program that finds all sequences of 6 consecutive prime 5-digit numbers, so of the form (a, b, c, d, e, f) with b = a + 2, c = b + 4, d = c + 6, e = d + 8, and f = e + 10. So a, b, c, d and e are all 5-digit prime numbers and no number between a and b, between b and c, between c and d, between d and e, and between e and f is prime.

The expected output is:

The solutions are:

13901	13903	13907	13913	13921	13931
21557	21559	21563	21569	21577	21587
28277	28279	28283	28289	28297	28307
55661	55663	55667	55673	55681	55691
68897	68899	68903	68909	68917	68927

2 C Decoding a multiplication

Write a program that decodes all multiplications of the form



such that the sum of all digits in all 4 columns is constant.

The expected output is:

411 * 13 = 5343, all columns adding up to 10. 425 * 23 = 9775, all columns adding up to 18.

3 Finding particular sequences of triples

Write a program that finds all triples of positive integers (i, j, k) such that i, j and k are two digit numbers, no digit occurs more than once in i, j and k, and the set of digits that occur in i, j or k is equal to the set of digits that occur in the product of i, j and k.

The expected output is:

Consider writing two versions: one that uses the builtin set operator, and one that uses bitwise operators. So for instance, with respect to the solution $20 \times 79 \times 81 = 127980$,

- one version would build the sets {0,2}, {0,2,7,9}, {0,1,2,7,8,9}, verify that they are of respective sizes 2, 4 and 6, and verify that the latter is equal to the set of digits occurring in the product, 127980;
- another version would build the integers 2⁰ + 2², 2⁰ + 2² + 2⁷ + 2⁹, 2⁰ + 2¹ + 2² + 2⁷ + 2⁸ + 2⁹, verify that the number of bits set to 1 in these integers is equal to 2, 4 and 6, respectively, and verify that the set of bits set to 1 in the third of these three integers is equal to the set of bits set to 1 in the product, 127980.

4 Decoding a sequence of operations

Write a program that finds all possible ways of inserting + and - signs in the sequence 123456789 (at most one sign before any digit) such that the resulting arithmetic expression evaluates to 100.

Here are a few hints.

- 1 can either be preceded by -, or optionally be preceded by +; so 1 starts a negative or a positive number.
- All other digits can be preceded by and start a new number to be subtracted to the running sum, or be preceded by + and start a new number to be added to the running sum, or not be preceded by any sign and be part of a number which it is not the leftmost digit of. That gives 3^8 possibilities for all digits from 2 to 9. We can generate a number N in $[0, 3^8 1]$. Then we can:
 - consider the remainder division of N by 3 to decide which of the three possibilities applies to 2;
 - consider the remainder division of $\frac{N}{3}$ by 3 to decide which of the three possibilities applies to 3;
 - consider the remainder division of $\frac{N}{3^2}$ by 3 to decide which of the three possibilities applies to 4;
 - ...

The expected output is (the ordering could be different):

1 + 23 - 4 + 5 + 6 + 78 - 9 = 100 123 - 4 - 5 - 6 - 7 + 8 - 9 = 100 123 + 45 - 67 + 8 - 9 = 100 123 + 4 - 5 + 67 - 89 = 100 12 + 3 + 4 + 5 - 6 - 7 + 89 = 100 123 - 45 - 67 + 89 = 100 12 - 3 - 4 + 5 - 6 + 7 + 89 = 100 1 + 2 + 34 - 5 + 67 - 8 + 9 = 100 1 + 2 + 3 - 4 + 5 + 6 + 78 + 9 = 100 12 + 3 - 4 + 5 + 6 + 78 + 9 = 100 12 + 3 - 4 + 5 + 67 + 8 + 9 = 100 12 + 3 - 4 + 5 + 67 + 8 + 9 = 100 1 + 23 - 4 + 56 + 7 + 8 + 9 = 100

Consider writing two versions: one that generates and evaluates the expression on the left hand side of the equality "by hand", and one that generates and evaluates the expression on the left hand side of the equality using the builtin eval() function.