## Knowledge engineering

## KR is first and foremost about knowledge

meaning and entailment
find individuals and properties, then encode facts sufficient for entailments

Before implementing, need to understand clearly

- what is to be computed?
- why and where inference is necessary?


## Example domain: soap-opera world

people, places, companies, marriages, divorces, hanky-panky, deaths, crimes, ...

## Task: KB with appropriate entailments

- what vocabulary?
- what facts to represent?


## Vocabulary

## Domain-dependent predicates and functions

main question:
what are the individuals?
here: people, places, companies, ...

## named individuals

john, sleezyTown, faultyInsuranceCorp, fic, johnQsmith, ...

## basic types

Person, Place, Man, Woman, ...

## attributes

Rich, Beautiful, Unscrupulous, ...

## relationships

LivesAt, MarriedTo, DaughterOf, HairDresserOf, HadAnAffairWith, Blackmails, ...

## functions

fatherOf, ceoOf, bestFriendOf, ...

## Basic facts

## Usually atomic sentences and negations

## type facts

Man(john),
Woman(jane),
Company(faultyInsuranceCorp)
property facts
Rich(john),
$\neg$ HappilyMarried(jim),
WorksFor(jim,fic)
equality facts
john $=$ ceoOf(fic),
fic = faultyInsuranceCorp,
bestFriendOf(jim) = john

## Like a simple database

could store these facts in relational tables

## Complex facts

## Universal abbreviations

$\forall y[\operatorname{Woman}(y) \wedge y \neq$ jane $\supset \operatorname{Loves}(y, j o h n)]$
$\forall y[\operatorname{Rich}(y) \wedge \operatorname{Man}(y) \supset \operatorname{Loves}(y, j a n e)]$
$\forall x \forall y[\operatorname{Loves}(x, y) \supset \neg \operatorname{Blackmails}(x, y)]$
possible to express without quantifiers

## Incomplete knowledge

Loves(jane,john) v Loves(jane,jim) which?
$\exists x[\operatorname{Adult}(x) \wedge \operatorname{Blackmails}(x$, john $)]$
who?
cannot write down more complete version

## Closure axioms

$\forall x[\operatorname{Person}(x) \supset x=j a n e \vee x=j o h n \vee x=j i m \ldots]$
$\forall x \forall y[\operatorname{MarriedTo}(x, y) \supset \ldots]$
$\forall x[x=$ fic $\vee x=$ jane $\vee x=$ john $\vee x=j i m \ldots]$
limits domain of discourse
also useful to have jane $\neq$ john ...

## Terminological facts

General relationships among predicates. For example:
disjoint

$$
\forall x[\operatorname{Man}(x) \supset \neg \operatorname{Woman}(x)]
$$

subtype
$\forall x[$ Senator $(x) \supset$ Legislator $(x)]$
exhaustive

$$
\forall x[\operatorname{Adult}(x) \supset \operatorname{Man}(x) \vee \operatorname{Woman}(x)]
$$

symmetry
$\forall x \forall y[\operatorname{MarriedTo}(x, y) \supset \operatorname{MarriedTo}(y, x)]$
inverse

$$
\forall x \forall y[\operatorname{ChildOf}(x, y) \supset \operatorname{ParentOf}(y, x)]
$$

## type restriction

$\forall x \forall y[\operatorname{MarriedTo}(x, y) \supset$
$\operatorname{Person}(x) \wedge \operatorname{Person}(y)]$
full definition

$$
\forall x[\operatorname{Rich} \operatorname{Man}(x) \equiv \operatorname{Rich}(x) \operatorname{Man}(x)]
$$

Usually universally quantified conditionals or biconditionals

## Entailments: 1

## Is there a company whose CEO loves Jane?

## $\exists x[\operatorname{Company}(x) \wedge \operatorname{Loves}(\operatorname{ceoOf}(x)$,jane $)]$ ??

Suppose $I \mid=$ KB.
Then $\boldsymbol{I} \mid=\operatorname{Rich}(j o h n), \operatorname{Man}(j o h n)$,
and $\boldsymbol{I} \mid=\forall y[\operatorname{Rich}(y) \wedge \operatorname{Man}(y) \supset \operatorname{Loves}(y, j a n e)]$
so $\boldsymbol{I} \mid=\operatorname{Loves(john,jane).~}$
Also $\boldsymbol{I} \mid=$ john $=\operatorname{ceoOf}(f i c)$,
so $\boldsymbol{I} \mid=\operatorname{Loves}(\operatorname{ceoOf}(f i c)$,jane $)$.
Finally $\boldsymbol{I} \mid=$ Company(faultyInsuranceCorp),
and $\boldsymbol{I} \mid=$ fic = faultyInsuranceCorp,
so $\boldsymbol{I} \mid=$ Company(fic).
Thus, $\boldsymbol{I} \mid=$ Company(fic) ^ Loves( ceoOf(fic),jane),

## and so

$$
\boldsymbol{I} \mid=\exists x[\operatorname{Company}(x) \wedge \operatorname{Loves}(\operatorname{ceoOf}(x), j a n e)] .
$$

Can extract identity of company from this proof

## Entailments: 2

## If no man is blackmailing John, then is he being blackmailed by somebody he loves?

$\forall x[\operatorname{Man}(x) \supset \neg \operatorname{Blackmails}(x$, john $)] \supset$
$\exists y[\operatorname{Loves(john,y)~\wedge ~Blackmails(y,john)]~??~}$
Note: $\mathrm{KB} \mid=(\alpha \supset \beta)$ iff $\mathrm{KB} \cup\{\alpha\} \mid=\beta$
Assume: $\boldsymbol{I} \mid=\mathrm{KB} \cup\{\forall x[\operatorname{Man}(x) \supset \neg \operatorname{Blackmails}(x$, john $)]\}$
Show: $\boldsymbol{I} \mid=\exists y[\operatorname{Loves}(j o h n, y) \wedge$ Blackmails $(y, j o h n)$

| Have: and | $\exists x[\operatorname{Adult}(x) \wedge$ Blackmails $(x$, john $)]$ $\forall x[\operatorname{Adult}(x) \supset \operatorname{Man}(x) \vee \operatorname{Woman}(x)]$ |
| :---: | :---: |
| so | $\exists x[\operatorname{Woman}(x) \wedge \operatorname{Blackmails}(x$,john $)]$. |
| Then: and so | $\forall y[\operatorname{Rich}(y) \wedge \operatorname{Man}(y) \supset \operatorname{Loves}(y, j a n e)]$ Rich(john) ^ Man(john) Loves(john,jane)! |
| But: <br> and <br> so <br> and... | $\forall y[\operatorname{Woman}(y) \wedge y \neq \operatorname{jane} \supset \operatorname{Loves}(y, j o h n)]$ <br> $\forall x \forall y[\operatorname{Loves}(x, y) \supset \neg \operatorname{Blackmails}(x, y)]$ <br> $\forall y[\operatorname{Woman}(y) \wedge y \neq$ jane $\supset \neg \operatorname{Blackmails}(y, \mathrm{john})]$ <br> Blackmails(jane,john)!! |

Finally: Loves(john,jane) ^ Blackmails(jane,john)
so:
$\exists y[\operatorname{Loves}(j o h n, y) \wedge$ Blackmails( $y$,john)]

## Proof as sequence of sentences

## What individuals?

## Sometimes useful to reduce n -ary predicates to 1 -place predicates and 1-place functions

- involves reifying properties: new individuals
- typical of description logics / frame languages


## Flexibility in terms of arity:

Purchases(john,sears,bike) or
Purchases(john,sears,bike,feb14) or
Purchases(john,sears,bike,feb14,\$100)

Instead introduce purchase objects
$\operatorname{Purchase}(p) \wedge \operatorname{agent}(p)=$ john $\wedge$
$\operatorname{obj}(p)=$ bike $\wedge \operatorname{source}(p)=$ sears $\wedge$ amount $(p)=\ldots$ ^...
allows purchase to be described at various levels of detail

## Complex relationships:

MarriedTo $(x, y) \quad$ vs.
PreviouslyMarriedTo $(x, y) \quad$ vs.
$\operatorname{ReMarriedTo}(x, y)$
Define marital status in terms of existence of marriages and divorces.

```
Marriage(m) ^ husband(m)=x ^
wife}(m)=y ^ date(m)=\ldots ^
witness}(m)=... ^ ..
```


## Abstract individuals

Also need individuals for numbers, dates, times, addresses, etc.
objects about which we ask wh-questions

## Quantities as individuals

$$
\begin{aligned}
& \operatorname{age}(\text { suzy })=14 \\
& \text { age-in-years }(\text { suzy })=14 \\
& \text { age-in-months(suzy })=168
\end{aligned}
$$

perhaps better to have an object for the age of Suzy, whose value in years is 14

$$
\begin{aligned}
& \operatorname{years}(\operatorname{age}(\operatorname{suzy}))=14 \\
& \operatorname{months}(x)=12 * \operatorname{years}(x) \\
& \operatorname{centimeters}(x)=100 * \operatorname{meters}(x)
\end{aligned}
$$

## Similarly with locations and times

instead of

$$
\text { time }(m)=" J a n ~ 51992 \text { 4:47:03EST" }
$$

can use

$$
\operatorname{time}(m)=t \wedge \operatorname{year}(t)=1992 \wedge \ldots
$$

## Other sorts of facts

## Statistical / probabilistic facts

- Half of the companies are located on the East Side.
- Most of the employees are restless.
- Almost none of the employees are completely trustworthy,


## Default / prototypical facts

- Company presidents typically have secretaries intercepting their phone calls.
- Cars have four wheels.
- Companies generally do not allow employees that work together to be married.


## Intentional facts

- John believes that Henry is trying to blackmail him.
- Jane does not want Jim to think that she loves John.


## Others ...

