COMP9444 19t3

# COMP9444 Neural Networks and Deep Learning

# 2a. Backpropagation

#### Textbook, Sections 3.10, 4.3, 5.1-5.2, 6.5.2

> agent is presented with examples of inputs and their target outputs

> agent is not presented with target outputs, but is given a reward

> agent is only presented with the inputs themselves, and aims to

Types of Learning (5.1)

signal, which it aims to maximize

find structure in these inputs

Supervised Learning

Reinforcement Learning

Unsupervised Learning

#### Outline

- Supervised Learning (5.1)
- Ockham's Razor (5.2)
- Multi-Layer Networks
- Continuous Activation Functions (3.10)
- Gradient Descent (4.3)
- Backpropagation (6.5.2)

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### Supervised Learning

- we have a training set and a test set, each consisting of a set of items; for each item, a number of input attributes and a target value are specified.
- the aim is to predict the target value, based on the input attributes.
- agent is presented with the input and target output for each item in the training set; it must then predict the output for each item in the test set
- various learning paradigms are available:
  - Neural Network
  - Decision Tree
  - ▶ Support Vector Machine, etc.

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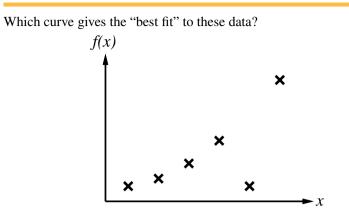
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## Supervised Learning – Issues

- framework (decision tree, neural network, SVM, etc.)
- representation (of inputs and outputs)
- pre-processing / post-processing
- training method (perceptron learning, backpropagation, etc.)
- generalization (avoid over-fitting)
- evaluation (separate training and testing sets)

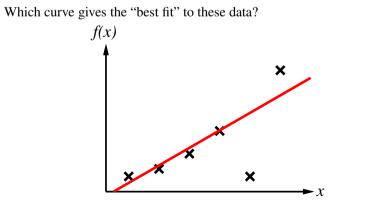


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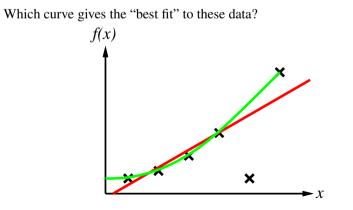
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## **Curve Fitting**



straight line?

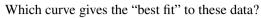
### **Curve Fitting**

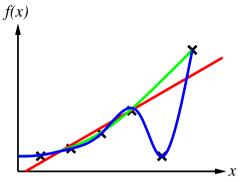


parabola?

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### **Curve Fitting**



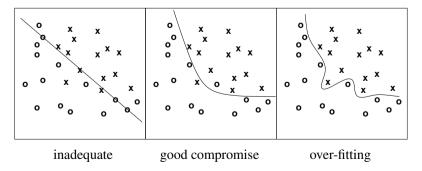


4th order polynomial?

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#### **Ockham's Razor (5.2)**

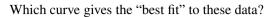
"The most likely hypothesis is the simplest one consistent with the data."

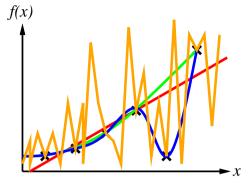


Since there can be noise in the measurements, in practice need to make a tradeoff between simplicity of the hypothesis and how well it fits the data.

## **Curve Fitting**

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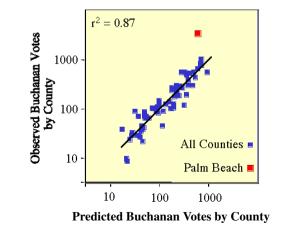




#### Something else?

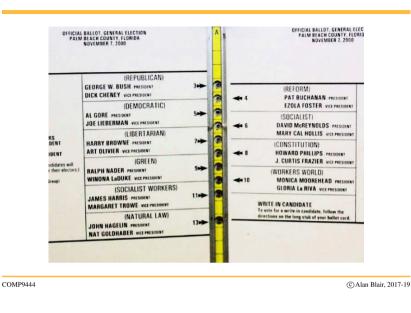
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## **Outliers**



[faculty.washington.edu/mtbrett]

### **Butterfly Ballot**

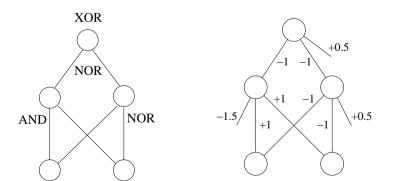


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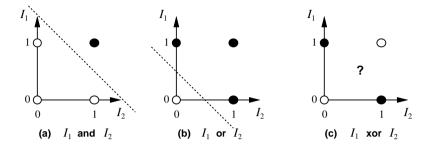
## **Multi-Layer Neural Networks**



Problem: How can we train it to learn a new function? (credit assignment)

## **Recall: Limitations of Perceptrons**

Problem: many useful functions are not linearly separable (e.g. XOR)



#### Possible solution:

 $x_1$  XOR  $x_2$  can be written as:  $(x_1 \text{ AND } x_2) \text{ NOR } (x_1 \text{ NOR } x_2)$ 

Recall that AND, OR and NOR can be implemented by perceptrons.

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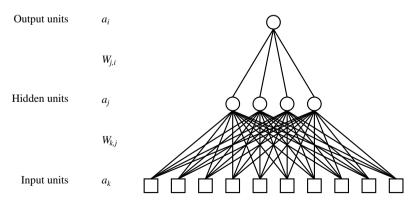
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## **Two-Layer Neural Network**



Normally, the numbers of input and output units are fixed, but we can choose the number of hidden units.

#### **The XOR Problem**

<i>x</i> <sub>1</sub>	<i>x</i> <sub>2</sub>	target	
0	0	0	
0	1	1	
1	0	1	
1	1	0	

- for this toy problem, there is only a training set; there is no validation or test set, so we don't worry about overfitting
- the XOR data cannot be learned with a perceptron, but can be achieved using a 2-layer network with two hidden units

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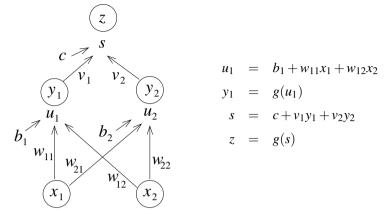
#### **NN Training as Cost Minimization**

We define an **error** function or **loss** function *E* to be (half) the sum over all input patterns of the square of the difference between actual output and target output

$$E = \frac{1}{2} \sum_{i} (z_i - t_i)^2$$

If we think of *E* as height, it defines an error **landscape** on the weight space. The aim is to find a set of weights for which E is very low.

#### **Neural Network Equations**



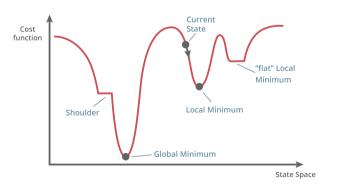
We sometimes use w as a shorthand for any of the trainable weights  $\{c, v_1, v_2, b_1, b_2, w_{11}, w_{21}, w_{12}, w_{22}\}.$ 

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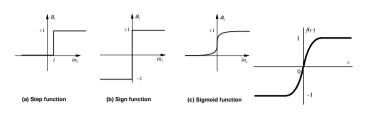
## Local Search in Weight Space



Problem: because of the step function, the landscape will not be smooth but will instead consist almost entirely of flat local regions and "shoulders", with occasional discontinuous jumps.

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Key Idea: Replace the (discontinuous) step function with a differentiable function, such as the sigmoid:

 $g(s) = \frac{1}{1 + e^{-s}}$ 

or hyperbolic tangent

$$g(s) = \tanh(s) = \frac{e^s - e^{-s}}{e^s + e^{-s}} = 2\left(\frac{1}{1 + e^{-2s}}\right) - 1$$

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#### **Chain Rule (6.5.2)**

If, say

y = y(u)u = u(x)

Then

$$\frac{\partial y}{\partial x} = \frac{\partial y}{\partial u} \frac{\partial u}{\partial x}$$

This principle can be used to compute the partial derivatives in an efficient and localized manner. Note that the transfer function must be differentiable (usually sigmoid, or tanh).

Note: if 
$$z(s) = \frac{1}{1 + e^{-s}}$$
,  $z'(s) = z(1 - z)$ .  
if  $z(s) = \tanh(s)$ ,  $z'(s) = 1 - z^2$ .

#### **Gradient Descent (4.3)**

Recall that the **loss** function E is (half) the sum over all input patterns of the square of the difference between actual output and target output

 $E = \frac{1}{2} \sum_{i} (z_i - t_i)^2$ 

The aim is to find a set of weights for which *E* is very low.

If the functions involved are smooth, we can use multi-variable calculus to adjust the weights in such a way as to take us in the steepest downhill direction.

$$w \leftarrow w - \eta \frac{\partial E}{\partial w}$$

Parameter  $\eta$  is called the learning rate.

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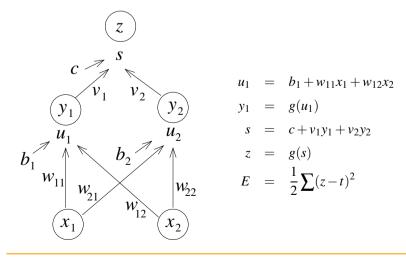
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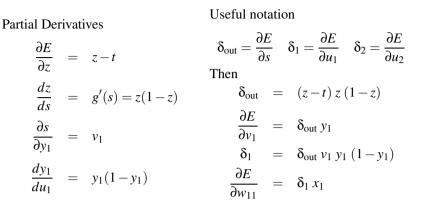
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### **Forward Pass**



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Partial derivatives can be calculated efficiently by packpropagating deltas through the network.

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#### **Example: Pima Indians Diabetes Dataset**

	Attribute	mean	stdv
1.	Number of times pregnant	3.8	3.4
2.	Plasma glucose concentration	120.9	32.0
3.	Diastolic blood pressure (mm Hg)	69.1	19.4
4.	Triceps skin fold thickness (mm)	20.5	16.0
5.	2-Hour serum insulin (mu U/ml)	79.8	115.2
6.	Body mass index (weight in kg/(height in m) <sup>2</sup> )	32.0	7.9
7.	Diabetes pedigree function	0.5	0.3
8.	Age (years)	33.2	11.8

Based on these inputs, try to predict whether the patient will develop Diabetes (1) or Not (0).

## Two-Layer NN's – Applications

	Medical Dignosis			
	Autonomous Driving			
	Game Playing			
	Credit Card Fraud Detection			
	Handwriting Recognition			
	Financial Prediction			
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## **Training Tips**

- re-scale inputs and outputs to be in the range 0 to 1 or -1 to 1
  - ▶ otherwise, backprop may put undue emphasis on larger values
- **replace missing values with mean value for that attribute**
- initialize weights to small random values
- on-line, batch, mini-batch, experience replay
- adjust learning rate (and momentum) to suit the particular task