COMP9444 Neural Networks and Deep Learning 6a. Recurrent Networks

Textbook, Chapter 10

COMP9444 © Alan Blair, 2017-19

COMP9444 19t3 Recurrent Networks 2 COMP9444 19t

Processing Temporal Sequences

There are many tasks which require a sequence of inputs to be processed rather than a single input.

- speech recognition
- time series prediction
- machine translation
- handwriting recognition

How can neural network models be adapted for these tasks?

COMP9444 19t3 Recurrent Networks

Outline

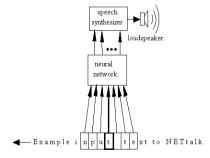
- Processing Temporal Sequences
- Sliding Window
- Recurrent Network Architectures
- Hidden Unit Dynamics
- Long Short Term Memory

COMP9444 © Alan Blair, 2017-19

COMP9444 19t3 Recurrent Networks 3

Sliding Window

COMP9444



The simplest way to feed temporal input to a neural network is the "sliding window" approach, first used in the NetTalk system (Sejnowski & Rosenberg, 1987).

NetTalk Task

Given a sequence of 7 characters, predict the phonetic pronunciation of the middle character.

For this task, we need to know the characters on both sides.

For example, how are the vowels in these words pronounced?

pa pat pate paternal

mo mod mode modern

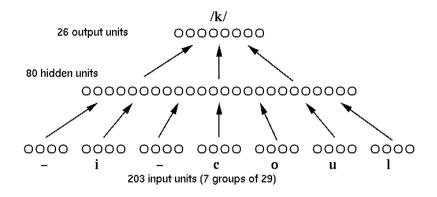
COMP9444 © Alan Blair, 2017-19

COMP9444 19t3 Recurrent Networks COMP9444 19t3 Recurrent Networks

NetTalk

- NETtalk gained a lot of media attention at the time.
- Hooking it up to a speech synthesizer was very cute. In the early stages of training, it sounded like a babbling baby. When fully trained, it pronounced the words mostly correctly (but sounded somewhat robotic).
- Later studies on similar tasks have often found that a decision tree could produce equally good or better accuracy.
- This kind of approach can only learn short term dependencies, not the medium or long term dependencies that are required for some tasks.

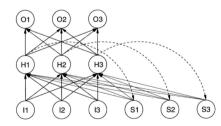
NetTalk Architecture



COMP9444 © Alan Blair, 2017-19

7

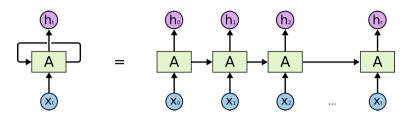
Simple Recurrent Network (Elman, 1990)



- at each time step, hidden layer activations are copied to "context" layer
- hidden layer receives connections from input and context layers
- the inputs are fed one at a time to the network, it uses the context layer to "remember" whatever information is required for it to produce the correct output

COMP9444 © Alan Blair, 2017-19 COMP9444 © Alan Blair, 2017-19

Back Propagation Through Time

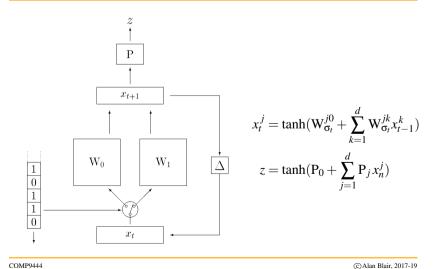


- we can "unroll" a recurrent architecture into an equivalent feedforward architecture, with shared weights
- applying backpropagation to the unrolled architecture is reffered to as "backpropagation through time"
- we can backpropagate just one timestep, or a fixed number of timesteps, or all the way back to beginning of the sequence

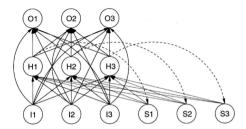
COMP9444 © Alan Blair, 2017-19

COMP9444 19t3 Recurrent Networks 10 COMP9444 19t3 Recurrent Networks 11

Second Order (or Gated) Networks



Other Recurrent Network Architectures



- it is sometimes beneficial to add "shortcut" connections directly from input to output
- connections from output back to hidden have also been explored (sometimes called "Jordan Networks")

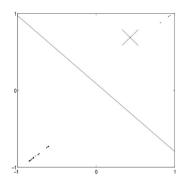
COMP9444 © Alan Blair, 2017-19

Task: Formal Language Recognition

Accept	Reject
1	0
1 1	1 0
1 1 1	0 1
1111	0 0
11111	0 1 1
111111	110
1111111	11111110
11111111	10111111

Scan a sequence of characters one at a time, then classify the sequence as Accept or Reject.

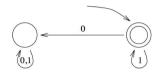
Dynamical Recognizers



$$W_0 = \begin{bmatrix} -0.89 & -0.09 & -0.14 \\ -1.13 & -0.09 & -0.14 \end{bmatrix}$$

$$W_1 = \begin{bmatrix} 0.20 & 0.68 & 0.96 \\ 0.20 & 0.81 & 1.19 \end{bmatrix}$$

$$P = \begin{bmatrix} -0.07 & 0.66 & 0.75 \end{bmatrix}$$



- gated network trained by BPTT
- emulates exactly the behaviour of Finite State Automaton

COMP9444

© Alan Blair, 2017-19

Task: Formal Language Recognition

Accept	Reject
1	000
0	11000
1 0	0001
0 1	000000000
0 0	11111000011
100100	1101010000010111
001111110100	1010010001
$0\ 1\ 0\ 0\ 1\ 0\ 0\ 1\ 0\ 0$	0000
1 1 1 0 0	00000
0010	

Scan a sequence of characters one at a time, then classify the sequence as Accept or Reject.

COMP9444

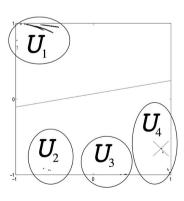
COMP9444

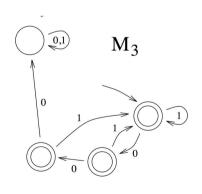
© Alan Blair, 2017-19

15

COMP9444 19t3 Recurrent Networks 14 COMP9444 19t3

Dynamical Recognizers

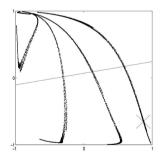




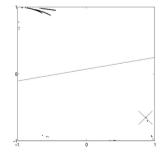
- trained network emulates the behaviour of Finite State Automaton
- training set must include short, medium and long examples

Recurrent Networks

Phase Transition



$$\begin{aligned} W_0 &= \begin{bmatrix} -0.567 & 1.761 & 0.815 \\ -0.219 & -2.591 & 0.446 \end{bmatrix} \\ W_1 &= \begin{bmatrix} 0.752 & 0.548 & -1.071 \\ 0.074 & -0.813 & 1.502 \end{bmatrix} \\ P &= \begin{bmatrix} 0.069 & 0.172 & -0.985 \end{bmatrix} \end{aligned}$$



$$W_0 = \begin{bmatrix} -0.567 & 1.763 & 0.816 \\ -0.219 & -2.593 & 0.446 \end{bmatrix}$$

$$W_1 = \begin{bmatrix} 0.751 & 0.549 & -1.073 \\ 0.075 & -0.813 & 1.502 \end{bmatrix}$$

$$P = \begin{bmatrix} 0.069 & 0.173 & -0.985 \end{bmatrix}$$

Chomsky Hierarchy

Language	Machine	Example
Regular	Finite State Automaton	a^n (n odd)
Context Free	Push Down Automaton	a^nb^n
Context Sensitive	Linear Bounded Automaton	$a^nb^nc^n$
Recursively Enumerable	Turing Machine	true QBF

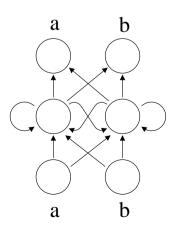
COMP9444 © Alan Blair, 2017-19

COMP9444 19t3 Recurrent Networks 18 COMP9444 19t3 Recurrent Networks 19

COMP9444

COMP9444

Elman Network for predicting a^nb^n

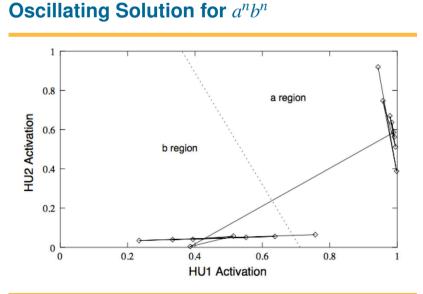


Task: Formal Language Prediction

Scan a sequence of characters one at a time, and try at each step to predict the next character in the sequence.

In some cases, the prediction is probabilistic.

For the a^nb^n task, the first b is not predictable, but subsequent b's and the initial a in the next subsequence are predictable.



COMP9444 © Alan Blair, 2017-19

© Alan Blair, 2017-19

© Alan Blair, 2017-19

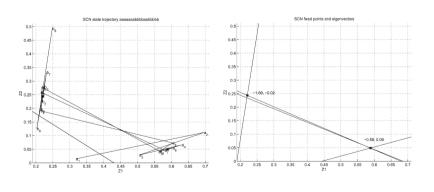
Learning to Predict a^nb^n

- the network does not implement a Finite State Automaton but instead uses two fixed points in activation space one attracting, the other repelling (Wiles & Elman, 1995)
- networks trained only up to $a^{10}b^{10}$ could generalize up to $a^{12}b^{12}$
- training the weights by evolution is more stable than by backpropagation
- networks trained by evolution were sometimes monotonic rather than oscillating

COMP9444 (C) Alan Blair, 2017-19

COMP9444 19t3 Recurrent Networks 22 COMP9444 19t3 Recurrent Networks 23

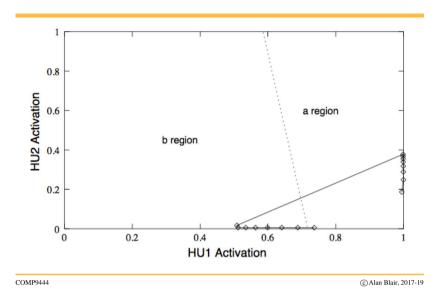
Hidden Unit Analysis for a^nb^n



hidden unit trajectory

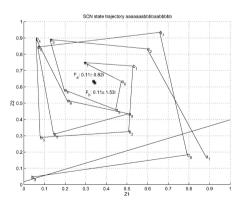
fixed points and eigenvectors

Monotonic Solution for a^nb^n



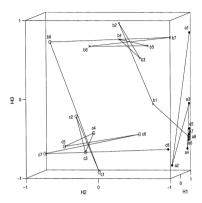
Counting by Spiralling

COMP9444



- for this task, sequence is accepted if the number of a's and b's are equal
- network counts up by spiralling inwards, down by spiralling outwards

Hidden Unit Dynamics for $a^nb^nc^n$



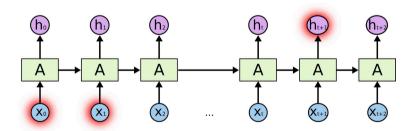
SRN with 3 hidden units can learn to predict $a^n b^n c^n$ by counting up and down simultaneously in different directions, thus producing a star shape.

COMP9444 © Alan Blair, 2017-19

COMP9444 19t3 Recurrent Networks 26 COMP9444 19t3 Recurrent Networks

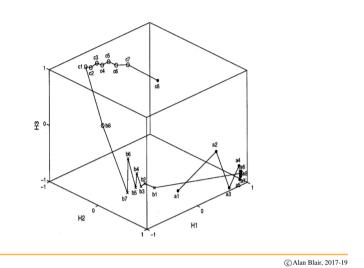
COMP9444

Long Range Dependencies



- Simple Recurrent Networks (SRNs) can learn medium-range dependencies but have difficulty learning long range dependencies
- Long Short Term Memory (LSTM) and Gated Recurrent Units (GRU) can learn long range dependencies better than SRN

Partly Monotonic Solution for $a^nb^nc^n$



27

Long Short Term Memory

Two excellent Web resources for LSTM:

http://colah.github.io/posts/2015-08-Understanding-LSTMs/ christianherta.de/lehre/dataScience/machineLearning/neuralNetworks/LSTM.php

COMP9444 © Alan Blair, 2017-19 COMP9444 © Alan Blair, 2017-19 COMP9444 19t3 Recurrent Networks

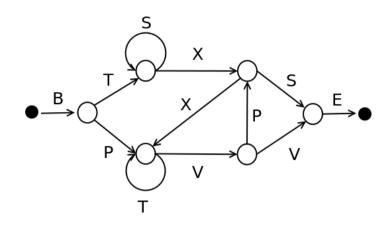
30

COMP9444 19t3

COMP9444

31

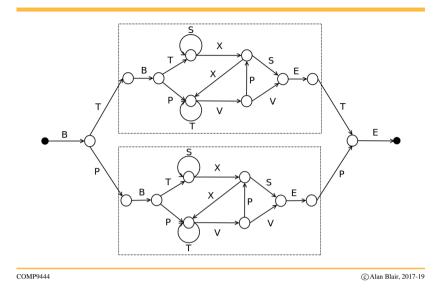
Reber Grammar



COMP9444 ©Alan Blair, 2017-19

Recurrent Networks

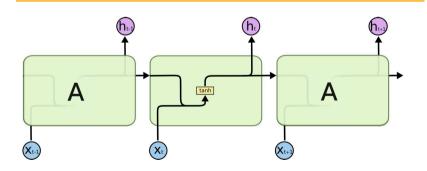
Embedded Reber Grammar



Recurrent Networks

Simple Recurrent Network

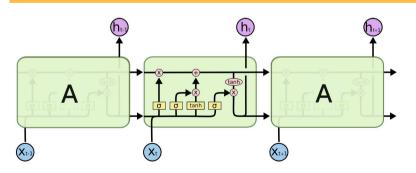
COMP9444 19t3



SRN – context layer is combined directly with the input to produce the next hidden layer.

SRN can learn Reber Grammar, but not Embedded Reber Grammar.

Long Short Term Memory



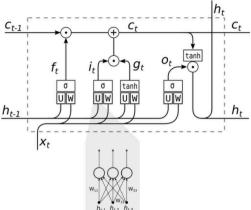
LSTM – context layer is modulated by three gating mechanisms: forget gate, input gate and output gate.

http://colah.github.io/posts/2015-08-Understanding-LSTMs/

COMP9444 © Alan Blair, 2017-19

© Alan Blair, 2017-19

Long Short Term Memory



COMP9444

Gates:

$$\begin{aligned} \mathbf{f}_t &= \sigma \left(W_f \mathbf{x}_t + U_f \mathbf{h}_{t-1} + \mathbf{b}_f \right) \\ \mathbf{i}_t &= \sigma \left(W_i \mathbf{x}_t + U_i \mathbf{h}_{t-1} + \mathbf{b}_i \right) \\ \mathbf{g}_t &= \tanh \left(W_g \mathbf{x}_t + U_g \mathbf{h}_{t-1} + \mathbf{b}_g \right) \\ \mathbf{o}_t &= \sigma \left(W_o \mathbf{x}_t + U_o \mathbf{h}_{t-1} + \mathbf{b}_o \right) \end{aligned}$$

© Alan Blair, 2017-19

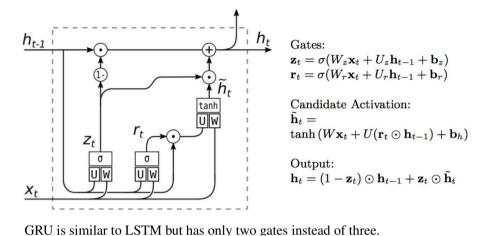
State:

$$\mathbf{c}_t = \mathbf{c}_{t-1} \odot \mathbf{f}_t + \mathbf{i}_t \odot \mathbf{g}_t$$

Output:

$$\mathbf{h}_t = \tanh \mathbf{c}_t \odot \mathbf{o}_t$$

Gated Recurrent Unit



COMP9444 © Alan Blair, 2017-19