COMP9444 20T3

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# **COMP9444 Neural Networks and Deep Learning**

## 9a. Autoencoders

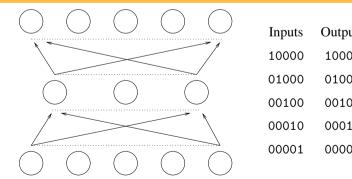
Textbook, Chapter 14

### **Outline**

- Autoencoder Networks (14.1)
- Regularized Autoencoders (14.2)
- Stochastic Encoders and Decoders (14.4)
- Generative Models
- Variational Autoencoders (20.10.3)

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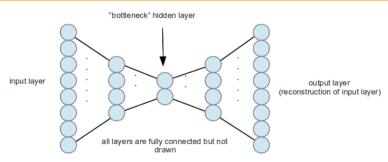
### **Recall: Encoder Networks**



Inputs	Outputs	
10000	10000	
01000	01000	
00100	00100	
00010	00010	
00001	00001	

- identity mapping through a bottleneck
- also called N–M–N task
- **used to investigate hidden unit representations**

### **Autoencoder Networks**



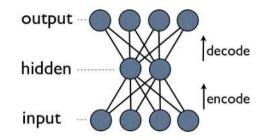
- output is trained to reproduce the input as closely as possible
- activations normally pass through a bottleneck, so the network is forced to compress the data in some way
- like the RBM, Autoencoders can be used to automatically extract abstract features from the input

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#### **Autoencoder Networks**



If the encoder computes z = f(x) and the decoder computes g(f(x)) then we aim to minimize some distance function between x and g(f(x))

E = L(x, g(f(x)))

#### Autoencoder as Pretraining

- after an autoencoder is trained, the decoder part can be removed and replaced with, for example, a classification layer
- this new network can then be trained by backpropagaiton
- the features learned by the autoencoder then serve as initial weights for the supervised learning task

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## Greedy Layerwise Pretraining

- Autoencoders can be used as an alternative to Restricted Bolzmann Machines, for greedy layerwise pretraining.
- An autoencoder with one hidden layer is trained to reconstruct the inputs. The first layer (encoder) of this network becomes the first layer of the deep network.
- Each subsequent layer is then trained to reconstruct the previous layer.
- A final classification layer is then added to the resulting deep network, and the whole thing is trained by backpropagation.

### Avoiding Trivial Identity

- If there are more hidden nodes than inputs (which often happens in image processing) there is a risk the network may learn a trivial identity mapping from input to output.
- We generally try to avoid this by introducing some form of regularization.

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### **Regularized Autoencoders (14.2)**

- autoencoders with dropout at hidden layer(s)
- sparse autoencoders
- contractive autoencoders
- denoising autoencoders

### Sparse Autoencoder (14.2.1)

- One way to regularize an autoencoder is to include a penalty term in the loss function, based on the hidden unit activations.
- This is analogous to the weight decay term we previously used for supervised learning.
- One popular choice is to penalize the sum of the absolute values of the activations in the hidden layer

$$E = L(x, g(f(x)) + \lambda \sum_{i} |h_i|$$

This is sometimes known as L<sub>1</sub>-regularization (because it involves the absolute value rather than the square); it can encourage some of the hidden units to go to zero, thus producing a sparse representation.

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### **Contractive Autoencoder (14.2.3)**

Another popular penalty term is the L<sub>2</sub>-norm of the derivatives of the hidden units with respect to the inputs

$$E = L(x, g(f(x)) + \lambda \sum_{i} ||\nabla_x h_i||^2$$

This forces the model to learn hidden features that do not change much when the training inputs x are slightly altered.

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### **Denoising Autoencoder (14.2.2)**

Another regularization method, similar to contractive autoencoder, is to add noise to the inputs, but train the network to recover the original input

```
repeat:
sample a training item x^{(i)}
generate a corrupted version \tilde{x} of x^{(i)}
train to reduce E = L(x^{(i)}, g(f(\tilde{x})))
end
```

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#### Loss Functions and Probability

- We saw previously how the loss (cost) function at the output of a feedforward neural network (with parameters  $\theta$ ) can be seen as defining a probability distribution  $p_{\theta}(x)$  over the outputs. We then train to maximize the log of the probability of the target values.
  - squared error assumes an underlying Gaussian distribution, whose mean is the output of the network
  - cross entropy assumes a Bernoulli distribution, with probability equal to the output of the network
  - softmax assumes a Boltzmann distribution

### **Stochastic Encoders and Decoders (14.4)**

- For autoencoders, the decoder can be seen as defining a conditional probability distribution  $p_{\theta}(x|z)$  of output *x* for a certain value *z* of the hidden or "latent" variables.
- In some cases, the encoder can also be seen as defining a conditional probability distribution  $q_{\phi}(z|x)$  of latent variables z based on an input x.
- We have seen an example of this with the Restricted Boltzmann Machine, where  $q_{\phi}(z|x)$  and  $p_{\theta}(x|z)$  are Bernoulli distributions.

Generative Mode	s		Gaussian Dis	stribution (3.9.3)	
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- Sometimes, as well as reproducing the training items {x<sup>(i)</sup>}, we also want to be able to use the decoder to generate new items which are of a similar "style" to the training items.
- In other words, we want to be able to choose latent variables z from a standard Normal distribution p(z), feed these values of z to the decoder, and have it produce a new item x which is somehow similar to the training items.
- Generative models can be:
  - explicit (Variational Autoencoders)
  - implicit (Generative Adversarial Networks)

 $\mu = \text{mean}$   $\sigma = \text{standard deviation}$ Multivariate Gaussian:  $P_{\mu,\sigma}(x) = \prod_{i} P_{\mu_i,\sigma_i}(x_i)$ 

 $P_{\mu,\sigma}(x) = \frac{1}{\sqrt{2\pi\sigma}} e^{-(x-\mu)^2/2\sigma^2}$ 

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#### **Entropy and KL-Divergence**

- The entropy of a distribution q() is  $H(q) = \int_{\theta} q(\theta)(-\log q(\theta)) d\theta$
- In Information Theory, H(q) is the amount of information (bits) required to transmit a random sample from distribution q()
- For a Gaussian distribution,  $H(q) = \sum \log \sigma_i$

KL-Divergence 
$$D_{KL}(q || p) = \int_{\theta} q(\theta) (\log q(\theta) - \log p(\theta)) d\theta$$

- **D**<sub>KL</sub> $(q \parallel p)$  is the number of extra bits we need to trasmit if we designed a code for p() but the samples are drawn from q() instead.
- If p(z) is Standard Normal distribution, minimizing  $D_{\text{KL}}(q_{\phi}(z) || p(z))$  encourages  $q_{\phi}()$  to center on zero and spread out to approximate p().

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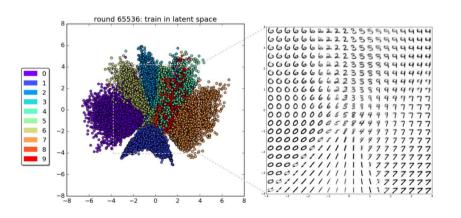
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### Variational Autoencoder Digits



### Variational Autoencoder (20.10.3)

Instead of producing a single z for each  $x^{(i)}$ , the encoder (with parameters  $\phi$ ) can be made to produce a mean  $\mu_{z|x^{(i)}}$  and standard deviation  $\sigma_{z|x^{(i)}}$ This defines a conditional (Gaussian) probability distribution  $q_{\phi}(z|x^{(i)})$ We then train the system to maximize

$$\mathbf{E}_{z \sim q_{\phi}(z|x^{(i)})}[\log p_{\theta}(x^{(i)}|z)] - D_{\mathrm{KL}}(q_{\phi}(z|x^{(i)}) \| p(z))$$

- the first term enforces that any sample z drawn from the conditional distribution q<sub>φ</sub>(z|x<sup>(i)</sup>) should, when fed to the decoder, produce somthing approximating x<sup>(i)</sup>
- the second term encourages  $q_{\phi}(z|x^{(i)})$  to approximate p(z)
- in practice, the distributions  $q_{\phi}(z|x^{(i)})$  for various  $x^{(i)}$  will occupy complementary regions within the overall distribution p(z)

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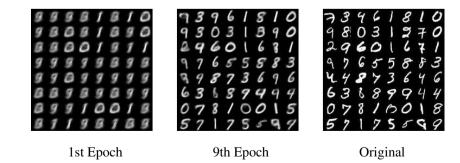
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### Variational Autoencoder Digits



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### **Variational Autoencoder Faces**



### **Variational Autoencoder**

- Variational Autoencoder produces reasonable results
- tends to produce blurry images
- $\blacksquare$  often end up using only a small number of the dimensions available to z

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### References

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