

Acknowledgement of Country

I would like to acknowledge and pay my respect to the Bedegal people who are the Traditional Custodians of the land on which UNSW is built, and of Elders past and present.

Meet the staff

I am **Paul Hunter**. I'm a lecturer at UNSW. My areas of interest are formal verification, graph theory and algorithms, lecturing, listing my interests. This is the first time I have taught this course.

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I am currently setting up Help sessions. These will be announced once I know the details. The staff will have taken the course before.

Contacting Us

`http://www.cse.unsw.edu.au/~cs3141`

Forum

There is an Ed forum linked on the course website (click [here](#) to join). Ask questions there. To avoid spoiling solutions, you can and should ask private questions.

Administrative questions should be sent to the course email










`cs3141@cse.unsw.edu.au`

Student Support

For help with anything else, there is always

Student Support - I Need Help With...

! Screenshot This Slide

Uni and Life in Australia Stress, Financial, Visas, Accommodation & More	 Student Support	student.unsw.edu.au/advisors
Reporting Sexual Assault/Harassment	 Equity Diversity and Inclusion (EDI)	edi.unsw.edu.au/sexual-misconduct
Educational Adjustments To Managemy Studies and Disability / Health Condition	 Equitable Learning Services (ELS)	student.unsw.edu.au/els
Academic and Study Skills	 Academic Skills	student.unsw.edu.au/skills
Special Consideration Because Life Impacts our Studies and Exams	 Special Consideration	student.unsw.edu.au/special-consideration
My Feelings and Mental Health Managing Low Mood, Unusual Feelings & Depression	 Mental Health Connect	student.unsw.edu.au/counselling Telehealth
	 Mind HUB	student.unsw.edu.au/mind-hub Online Self-Help Resources
	 In Australia Call Afterhours UNSW Mental Health Support Line	1300 787 026 5pm-9am
	 Outside Australia Afterhours 24-hour Medibank Hotline	+61 (2) 8905 0307

Safety-critical Applications

Think of the worst group assignment you ever had!

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- are logging into your online banking...
- are investing in a new hedge fund...
- are travelling in a self-driving car...
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... using software written by **your groupmates** from that group.

Safety-critical Example

What is wrong with this code:

Example

```
transfer(account to, account from, uint amount){  
  require (balances[from] > amount);  
  balancesFrom := balances[from] - amount;  
  balancesTo := balances[to] + amount;  
  balances[from] := balancesFrom;  
  balances[to] := balancesTo;  
}
```


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- **not** a programming languages course (see [COMP3161](#)).
- Certainly **not** a cakewalk; but hopefully **not** a soul-crushing nightmare either.

Assessment

Warning

For many of you, this course will present a lot of new topics. Even if you are a seasoned programmer, you may have to learn as if you were starting from scratch.

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- Class Marks (out of 100)
 - **Two** programming assignments, each worth 20 marks.
 - Weekly online quizzes, worth 20 marks.
 - Weekly programming exercises, worth 40 marks.
- Final Exam Marks (out of 100, **hurdle: 40**)

$$result = \frac{class + exam}{2}$$

Lectures

- **Lecture (Wed 11am-1pm):** I introduce new material.
- **Practical (Fri 11am-1pm):** Scott (usually) reinforces Wednesday's material with questions and examples.
- **Quiz:** due on Fri (one week after the lectures they examine), but **start early!**

Books

We won't set a textbook (a long COMP3141 tradition).

Resources: see the course outline for various books and online resources that are useful for learning Haskell.

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- You will learn a substantial amount of Haskell (we will provide some guidance). But the course is about learning techniques for mathematically structured programming.
- Based on feedback from previous iterations, I will endeavour to include examples from other languages.

About Haskell

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Warning

This means that some (possibly even most) tutorials, resources, answers you find on the Internet will be outdated!

Demo 1: Haskell Workflow

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Demo 1: Haskell Workflow

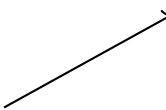
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Demo: GHCi, Modules

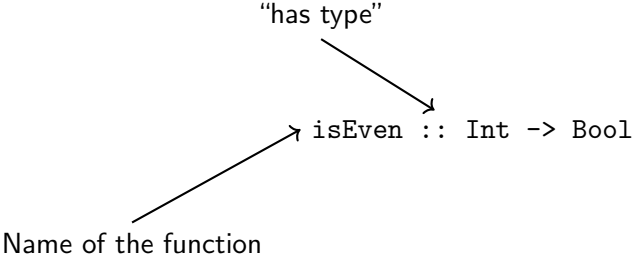
Demo 2: Declaring Functions

isEven :: Int -> Bool

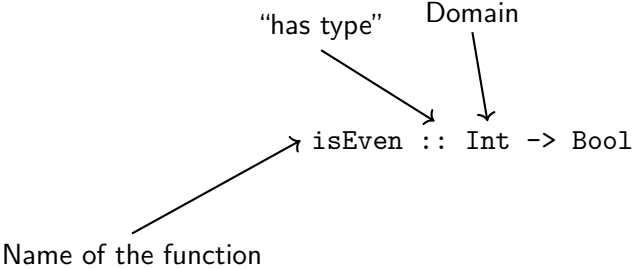
Name of the function



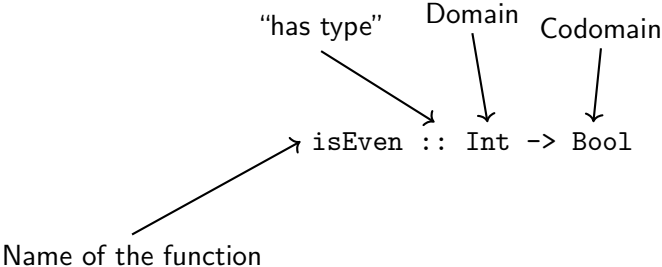
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Argument (Int) Result (Bool)



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isEven x = x 'mod' 2 == 0
```

Argument (Int) Result (Bool)

In mathematics, we would apply a function f to an argument x by writing $f(x)$. In Haskell we write `f x`, omitting the parentheses.

Demo: basic functions

Demo 3: Currying

- Haskell functions have one input domain and one output codomain. But some functions take multiple inputs.

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- Haskell functions have one input domain and one output codomain. But some functions take multiple inputs.
- In mathematics, we treat $\log_{10}(x)$ and $\log_2(x)$ and $\ln(x)$ as separate functions.
- In Haskell, we have a single function `logBase` that, given a number n , produces a function for $\log_n(x)$.

```
log10 :: Double -> Double  
log10 = logBase 10
```

```
log2 :: Double -> Double  
log2 = logBase 2
```

```
ln :: Double -> Double  
ln = logBase 2.71828
```

What's the **type** of `logBase`?

Demo 3: Currying

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logBase :: Double -> (Double -> Double)
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Function application associates to the **left** in Haskell, so:

$$\text{logBase } 2 \ 64 \equiv (\text{logBase } 2) \ 64$$

Demo: currying, multiple arguments

Demo 4: Tuples

We now know how to handle multiple inputs to a function? But what if we want to have multiple outputs?

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Haskell provides data types called tuples to handle multiple outputs:

```
neighbors :: Int -> (Int, Int)
```

```
neighbors x = (x - 1, x + 1)
```

Now, `(neighbors 1)` evaluates to `(0,2)`.

Demo: tuples

Demo 5: Higher Order Functions

In addition to returning functions, functions can take other functions as arguments:

```
applyTwice :: (t -> t) -> t -> t
applyTwice f x = f (f x)
```

```
square :: Int -> Int
square x = x * x
```

```
fourthPower :: Int -> Int
fourthPower = applyTwice square
```

Demo: higher-order functions, equational reasoning

Demo 6: Lists

Haskell makes extensive use of lists, constructed using square brackets. Each list element must be of the same type.

```
[True, False, True]   :: [Bool]
[3, 2, 5+1]           :: [Int]
[sin, cos]            :: [Double -> Double]
[ (3,'a'),(4,'b') ]   :: [(Int, Char)]
```

Demo 6: Lists

A useful function is `map`, which, given a function, applies it to each element of a list:

```
map not [True, False, True] = [False, True, False]
map square [3, -2, 4]       = [9, 4, 16]
map (\x -> x + 1) [1, 5]    = [2, 6]
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The last example here uses a *lambda expression* to define a one-use function without giving it a name.

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What's the type of `map`?

```
map :: (a -> b) -> [a] -> [b]
```

Demo 6: Lists

The type `String` in Haskell is just a list of characters:

```
type String = [Char]
```

This is a *type synonym*, like a `typedef` in C.

Thus:

```
"hi!" == ['h', 'i', '!']
```

Demo: lists

Word Frequencies

Let's solve a problem to get some practice implementing stuff:

Example (Task 1)

Given a number n and a string s containing English words, generate a report that lists the n most common words in the given string s .

I'll even give you an algorithm:

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Example (Task 1)

Given a number n and a string s containing English words, generate a report that lists the n most common words in the given string s .

I'll even give you an algorithm:

- 1 Break the input string into words.
- 2 Convert the words to lowercase.
- 3 Sort the words.
- 4 Group adjacent occurrences (runs) of the same word.
- 5 Sort runs words by length.
- 6 Take the longest n runs of the sorted list.
- 7 Generate a report.

Demo: word frequencies

The Dollar Pattern

We used *the dollar operator* `$` to reduce the use of parentheses.

- The dollar operator does normal function application, like `f x` (evaluation of a function at a value).
- However, while application has high operator precedence (“is done as early as possible”), the dollar operator has extremely low precedence (“is done as late as possible”).

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- `reverse [1,2,3] ++ [4]` results in `[3,2,1,4]`. The application of the `reverse` function binds very tightly, so we do it first, then concatenate.
- `reverse $ [1,2,3] ++ [4]` results in `[4,3,2,1]`. We concatenate first, then apply the reversing function. Same as `reverse ([1,2,3] ++ [4])`.

Function Composition

We used *function composition* to combine our functions together. The mathematical $(f \circ g)(x)$ is written $(f \ . \ g) \ x$ in Haskell.

In Haskell, operators like function composition are themselves functions. You can define your own!

```
-- Vector addition
```

```
(.+ ) :: (Int, Int) -> (Int, Int) -> (Int, Int)
```

```
(x1, y1) .+ (x2, y2) = (x1 + x2, y1 + y2)
```

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(2,3) .+ (1,1) == (3,4)
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```

You could even have defined function composition yourself if it didn't already exist:

```
(.) :: (b -> c) -> (a -> b) -> (a -> c)  
(f . g) x = f (g x)
```

Conditionals

Demo: polarity using guards, if statements.

Demo: (if we have time), loops via recursion.

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Lists are **singly-linked** lists in Haskell. The empty list is written as `[]` and a list node is written as `x : xs`. The value `x` is called the **head** and the rest of the list `xs` is called the **tail**. Thus:

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"hi!" == ['h', 'i', '!'] == 'h':('i':('!':[]))  
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```

When we define recursive functions on lists, we use the last form for pattern matching:

```
map :: (a -> b) -> [a] -> [b]  
map f []      = []  
map f (x:xs) = f x : map f xs
```

Equational Evaluation

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We can evaluate programs *equationally*:

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                  ≡ 'H' : 'I' : '!' : []
                  ≡ "HI!"
```

FIN

The quiz will be up on the course website sometime on Friday.

Warning

The quiz is assessed. The deadline is the end of next Friday.