

COMP9517: Computer Vision

Object Tracking

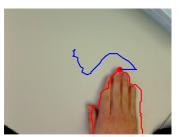
COMP9517 24T2W9 Object Tracking

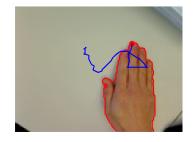
Motion Tracking

• Tracking is the problem of generating an inference about the motion of an object given a sequence of images









Applications

• Motion capture

- Record motion of people to control cartoon characters in animations
- Modify the motion record to obtain slightly different behaviours

Recognition from motion

- Determine the identity of a moving object
- Assess what the object is doing

Surveillance

- Detect and track objects in a scene for security
- Monitor their activities and warn if anything suspicious happens

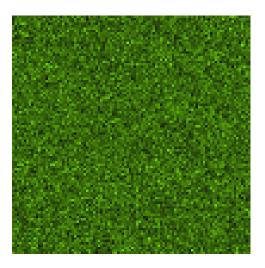
Targeting

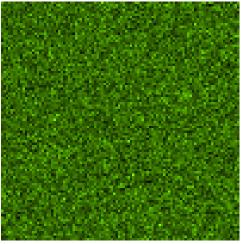
- Decide which objects to target in scene
- Make sure the objects get hit

Difficulties in Tracking

- Loss of information caused by projection of the 3D world on a 2D image
- Noise in images
- Complex object **motion**
- Non-rigid or articulated nature of objects
- Partial and full object occlusions
- Complex object shapes
- Scene illumination changes
- **Real-time** processing requirements

Example Tracking Problem





Single moving microscopic particle

Imaged with signal-to-noise ratio (SNR) of 1.5

Human visual motion perception

- Not so accurate and reproducible in quantification
- Good at integrating spatial and temporal information
- Powerful in making associations and predictions

Computer vision challenges

- Integration of spatial and temporal information
- Modeling and incorporation of prior knowledge
- Probabilistic rather than deterministic approach

Bayesian estimation methods...

Motion Assumptions

- When moving objects do not have unique texture or colour, the characteristics of the motion itself must be used to connect detected points into trajectories
- Assumptions about each moving object:
 - Location changes smoothly over time
 - Velocity (speed and direction) changes smoothly over time
 - Can be at only one location in space at any given time
 - Not in same location as another object at the same time

Topics

• Bayesian inference

Using *probabilistic models* to perform tracking

Kalman filtering

Using *linear model assumptions* for tracking

• Particle filtering

Using nonlinear models for tracking

Bayesian Inference

Problem Definition

- A moving object has a **state** which evolves over time Random variable: X_i can contain any quantities of interest (position, velocity, acceleration, shape, intensity, colour, ...)
- The state is **measured** at each time point Random variable: Y_i in computer vision the measurements are typically Specific value: Y_i features computed from the images
- Measurements are combined to estimate the state

Three Main Steps

• **Prediction**: use the measurements $(y_0, y_1, ..., y_{i-1})$ up to time i-1 to predict the state at time i

$$P(X_i | Y_0 = y_0, Y_1 = y_1, \dots, Y_{i-1} = y_{i-1})$$

- Association: select the measurements at time *i* that are related to the object state
- **Correction**: use the incoming measurement y_i to update the state prediction

$$P(X_i | Y_0 = y_0, Y_1 = y_1, \dots, Y_{i-1} = y_{i-1}, Y_i = y_i)$$

Independence Assumptions

• Current state depends only on the immediate past

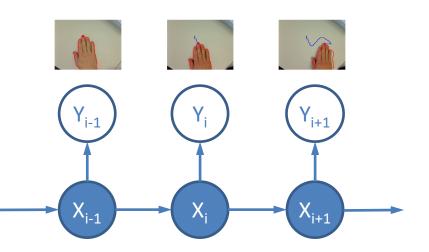
$$P(X_i | X_0, X_1, ..., X_{i-1}) = P(X_i | X_{i-1})$$

Measurements depend only on the current state

$$P(Y_i, Y_j, ..., Y_k | X_i) = P(Y_i | X_i) P(Y_j, ..., Y_k | X_i)$$

These assumptions imply the tracking problem has the structure of inference on a hidden Markov model

1



• Prediction

$$P(X_{i} | y_{0}, y_{1}, ..., y_{i-1}) = \int P(X_{i}, X_{i-1} | y_{0}, y_{1}, ..., y_{i-1}) dX_{i-1}$$

$$= \int P(X_{i} | X_{i-1}, y_{0}, y_{1}, ..., y_{i-1}) P(X_{i-1} | y_{0}, y_{1}, ..., y_{i-1}) dX_{i-1}$$

$$= \int P(X_{i} | X_{i-1}) P(X_{i-1} | y_{0}, y_{1}, ..., y_{i-1}) dX_{i-1}$$

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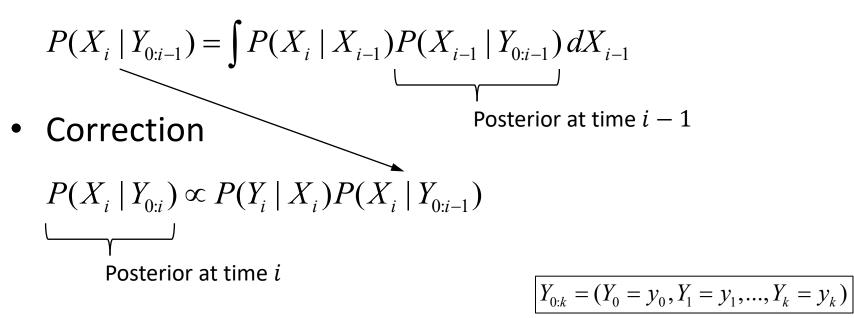
$$= \int P(X_{i} | X_{i-1}, y_{0}, y_{1}, ..., y_{i-1}) \frac{P(X_{i}, X_{i-1}, y_{0}, y_{1}, ..., y_{i-1})}{P(y_{0}, y_{1}, ..., y_{i-1})} \frac{P(X_{i} | X_{i-1}, y_{0}, y_{1}, ..., y_{i-1})}{P(y_{0}, y_{1}, ..., y_{i-1})} \frac{P(X_{i} | X_{i-1}, y_{0}, y_{1}, ..., y_{i-1})}{P(y_{0}, y_{1}, ..., y_{i-1})}$$

• Correction

$$\begin{split} P(X_{i} \mid y_{0}, y_{1}, ..., y_{i}) &= \frac{P(X_{i}, y_{0}, y_{1}, ..., y_{i})}{P(y_{0}, y_{1}, ..., y_{i})} \\ &= \frac{P(y_{i} \mid X_{i}, y_{0}, y_{1}, ..., y_{i-1})P(X_{i} \mid y_{0}, y_{1}, ..., y_{i-1})P(y_{0}, y_{1}, ..., y_{i-1})}{P(y_{0}, y_{1}, ..., y_{i})} \\ &= P(y_{i} \mid X_{i})P(X_{i} \mid y_{0}, y_{1}, ..., y_{i-1})\frac{P(y_{0}, y_{1}, ..., y_{i-1})}{P(y_{0}, y_{1}, ..., y_{i})} \\ &\propto P(y_{i} \mid X_{i})P(X_{i} \mid y_{0}, y_{1}, ..., y_{i-1}) \xrightarrow{} constant \\ measurement prediction of \\ model current state \end{split}$$

In summary, tracking by Bayesian inference is done by iterative prediction and correction:

• Prediction



To make tracking by Bayesian inference work in practice you need to design two models:

- Dynamics model $P(X_i | X_{i-1})$
- Measurement model $P(Y_i | X_i)$

The specific design choices are application dependent

Final estimates are computed from the posterior:

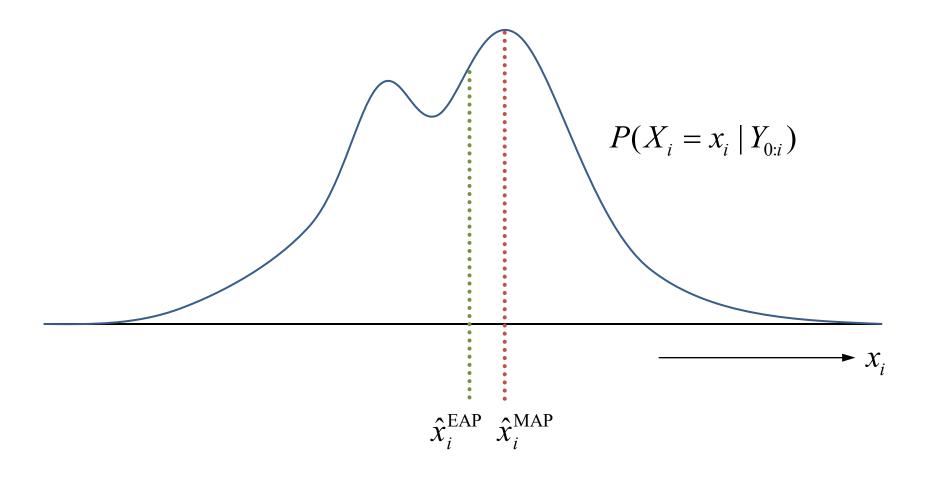
• Example 1: expected a posteriori (EAP)

$$\hat{x}_i = \int x_i P(X_i = x_i \mid Y_{0:i}) dx_i$$

• Example 2: maximum a posteriori (MAP)

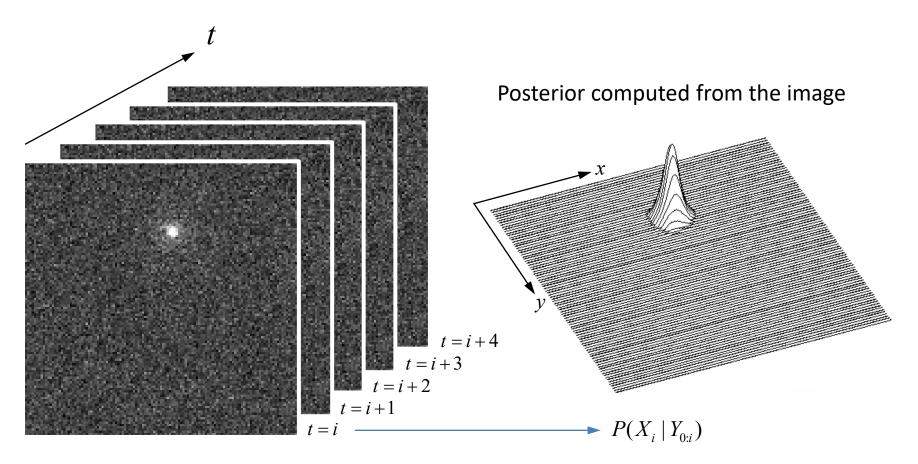
$$\hat{x}_i = \arg \max_{x_i} P(X_i = x_i | Y_{0:i})$$

These are the most popular ones but others are possible



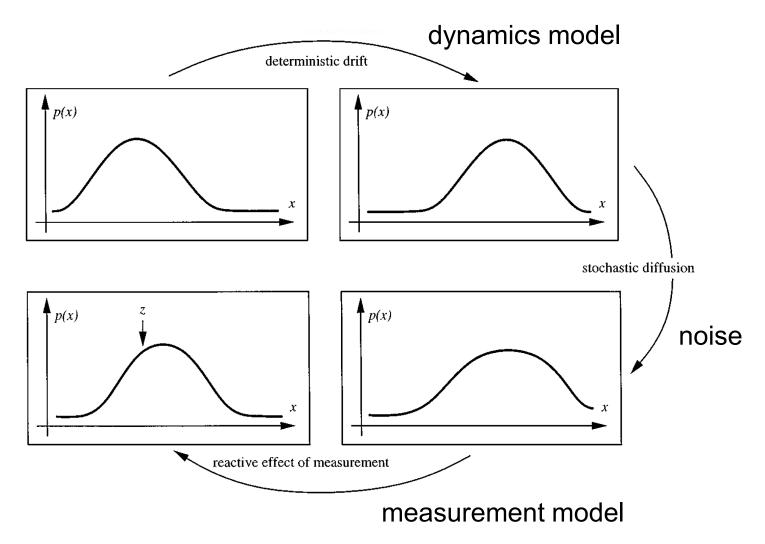
Bayesian Tracking Example

Estimating the coordinates of a moving particle:



Kalman Filtering

Probability Density Propagation



Linear / Gaussian Assumption

If we assume the dynamics (state transition) model and the measurement model to be linear, and the noise to be additive Gaussian, then all the probability densities will be Gaussians:

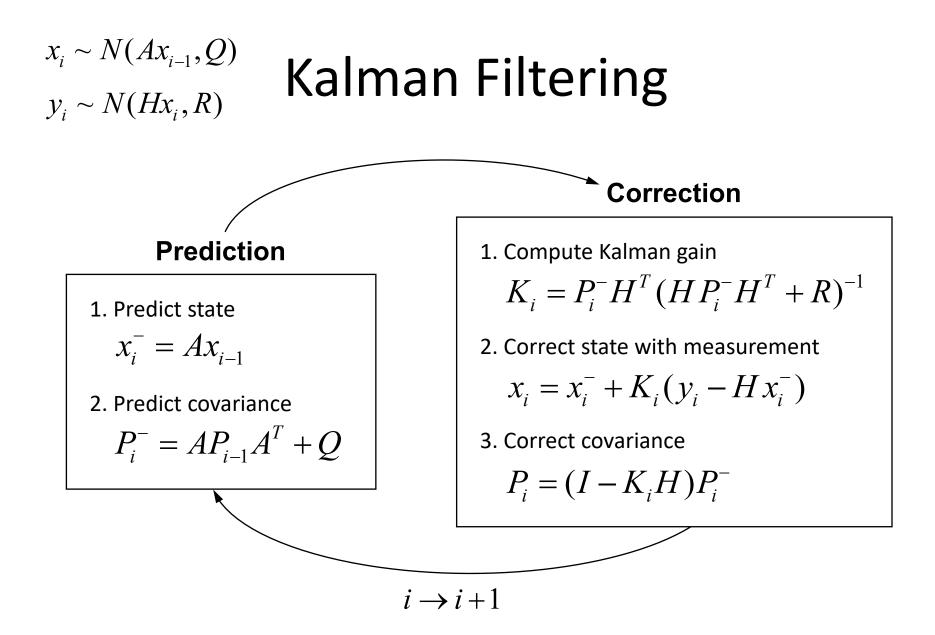
 $x \sim N(\mu, \Sigma)$

• The state is advanced by multiplying with some known matrix and then adding a zero-mean normal random variable:

$$x_i = Ax_{i-1} + q_{i-1}$$

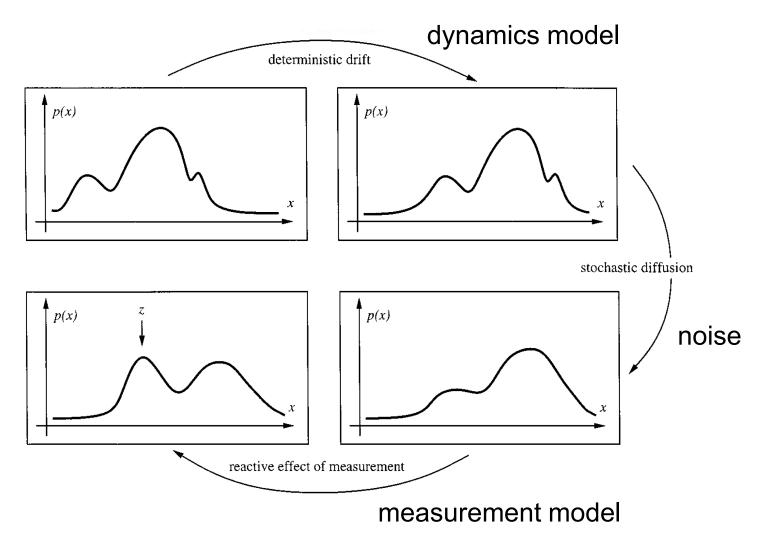
• The measurement is obtained by multiplying the state by some matrix and then adding a zero-mean normal random variable:

$$y_i = Hx_i + r_i$$



Particle Filtering

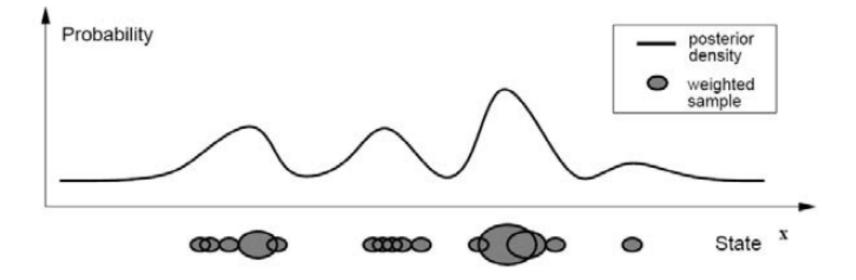
Probability Density Propagation



Non-Linear / Non-Gaussian Case

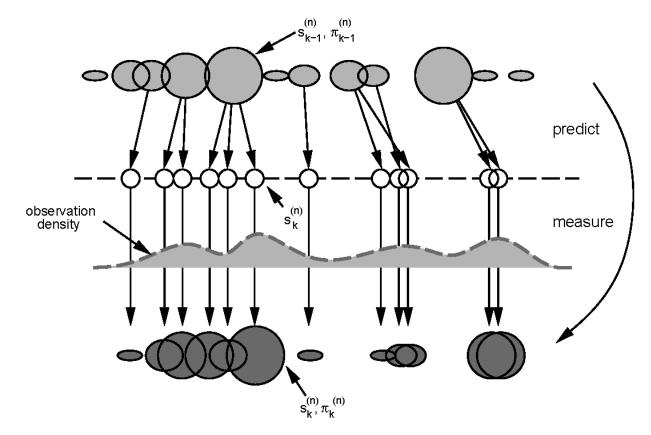
 Represent the conditional state density by a set of samples (particles) with corresponding weights (importance)

$$P(X_i | Y_{0:i}) \rightarrow \{s_i^{(n)}, \pi_i^{(n)}\}_{n=1}^N$$



Particle Filtering

 Propagate each sample using the dynamics model and obtain its new weight using the measurement model



Particle Filtering Algorithm

Iterate

From the "old" sample-set $\{\mathbf{s}_{t-1}^{(n)}, \pi_{t-1}^{(n)}, c_{t-1}^{(n)}, n = 1, \dots, N\}$ at time-step t-1, construct a "new" sample-set $\{\mathbf{s}_{t}^{(n)}, \pi_{t}^{(n)}, c_{t}^{(n)}\}, n = 1, \dots, N$ for time t.

Construct the n^{th} of N new samples as follows:

- 1. Select a sample $s'_t^{(n)}$ as follows:
 - (a) generate a random number $r \in [0, 1]$, uniformly distributed.
 - (b) find, by binary subdivision, the smallest j for which $c_{t-1}^{(j)} \ge r$

(c) set
$$s'_{t}^{(n)} = s^{(j)}_{t-1}$$

2. Predict by sampling from

$$p(\mathbf{x}_t | \mathbf{x}_{t-1} = \mathbf{s}'_{t-1}^{(n)})$$

to choose each $s_t^{(n)}$.

3. Measure and weight the new position in terms of the measured features z_t :

$$\pi_t^{(n)} = p(\mathbf{z}_t | \mathbf{x}_t = \mathbf{s}_t^{(n)})$$

then normalise so that $\sum_{n} \pi_t^{(n)} = 1$ and store together with cumulative probability as $(\mathbf{s}_t^{(n)}, \pi_t^{(n)}, c_t^{(n)})$ where

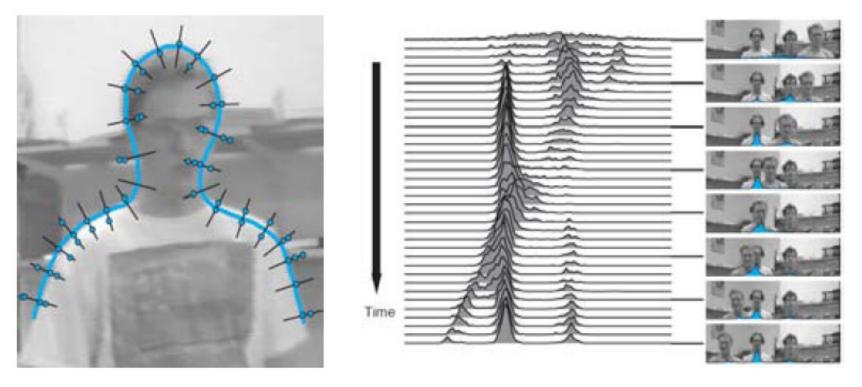
$$c_t^{(0)} = 0,$$

$$c_t^{(n)} = c_t^{(n-1)} + \pi_t^{(n)} \quad (n = 1...N)$$

NIPS 1996

Example Application

Tracking of active contour representations of objects



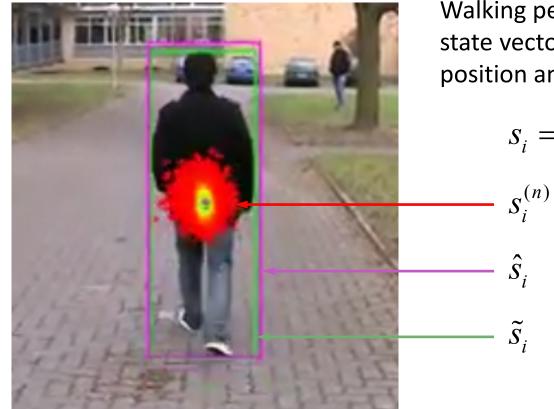
Particle filtering is also known variously as sequential Monte Carlo (SMC) filtering, bootstrap filtering, the condensation algorithm...

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Example Application

Tracking of object location in the presence of clutter



Walking pedestrian represented by a state vector consisting of a center position and a bounding box:

$$s_i = (x, y, w, h)_i$$

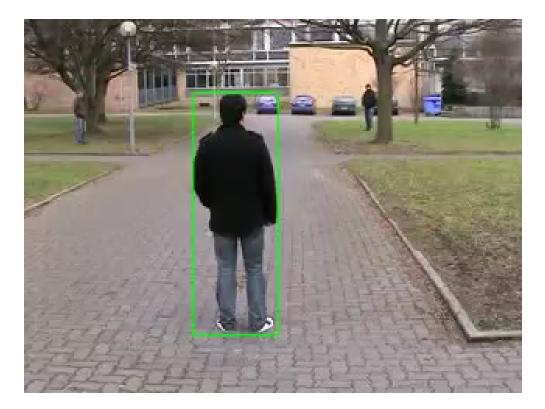
 $S_i^{(n)}$ (samples)

(estimated)

(truth/annotated)

Example Application

Tracking of object location in the presence of clutter



https://www.youtube.com/watch?v=j-duyzShJ_o

References and Acknowledgements

- Chapters 5 and 8 of Szeliski 2010
- Chapter 18 of Forsyth and Ponce 2011
- Chapter 9 of Shapiro and Stockman 2001
- Paper by M. Isard and A. Blake 1998 <u>CONDENSATION: Conditional density propagation for visual tracking</u> Available online via the UNSW Library
- Some images drawn from the above references

Example exam question

Which one of the following statements about object tracking is incorrect?

- A. The particle filtering method assumes that the dynamics model and the measurement model can be parameterized.
- B. The hidden Markov model assumes that the measurements depend only on the current state of the objects.
- C. The prediction step of Bayesian inference assumes that the current state of the objects depends only on the previous state.
- D. The Kalman filtering method assumes that the dynamics and measurement noise are additive Gaussian.